

Application of FDTD method for the Spatial Light Modulator (SLM)

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Project objective

1. Simulation : Investigation of influence of pixel geometry and fringe fields for SLM through robust electromagnetic wave model
2. Experiment : Investigation of polarization states of diffraction orders after propagation through SLM

Introduction

Spatial Light Modulator

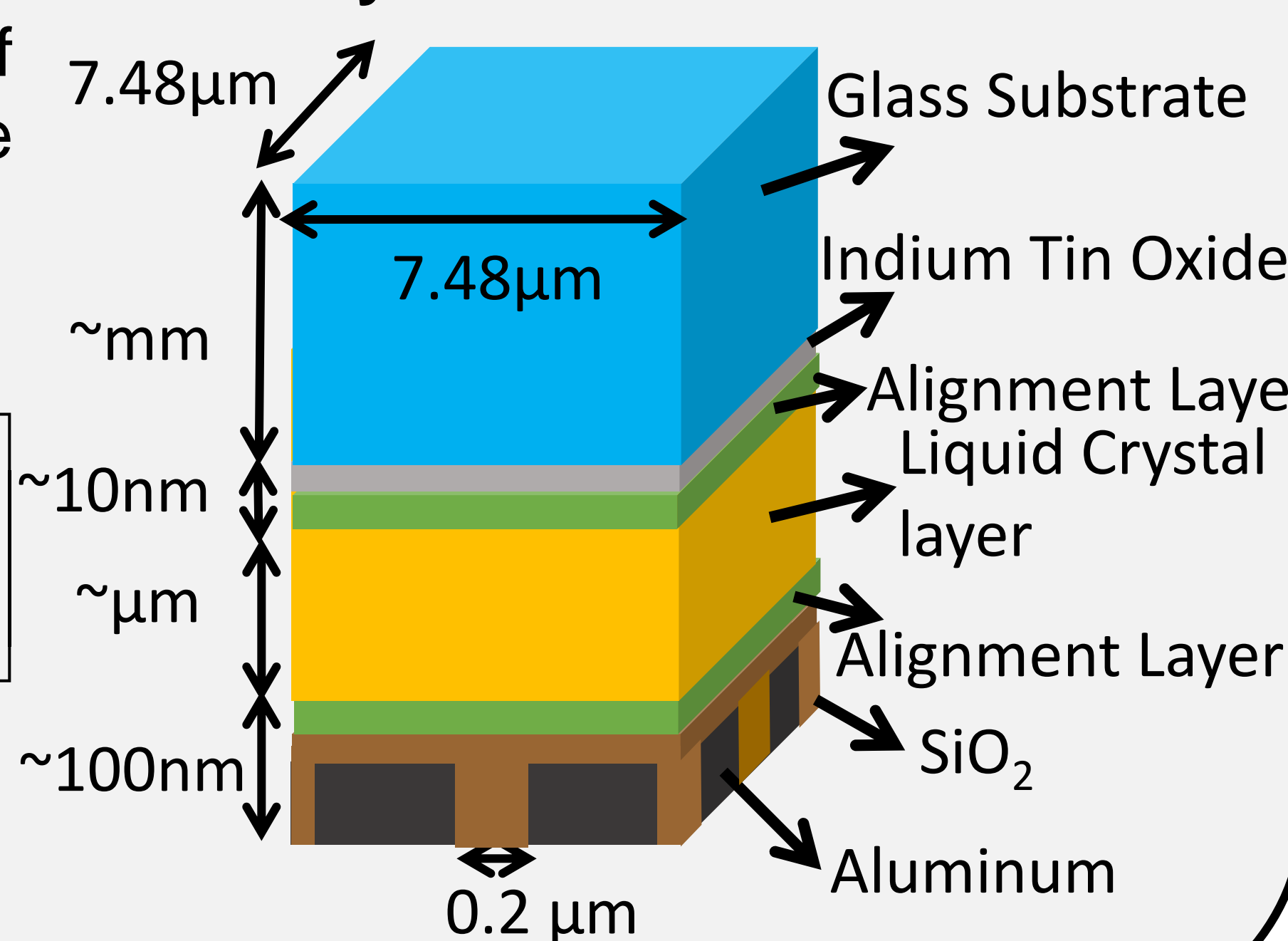
A device that can manipulate the phase of incident light via electrically adjusting the dielectric tensor of liquid crystal (LC).

Optical property of LC

$$\epsilon = \epsilon_0 \begin{bmatrix} n_x^2 & & \\ & n_y^2 & \\ & & n_z^2 \end{bmatrix} = \epsilon_0 \begin{bmatrix} n_o^2(V) & & \\ & n_e^2(V) & \\ & & n_o^2(V) \end{bmatrix}$$

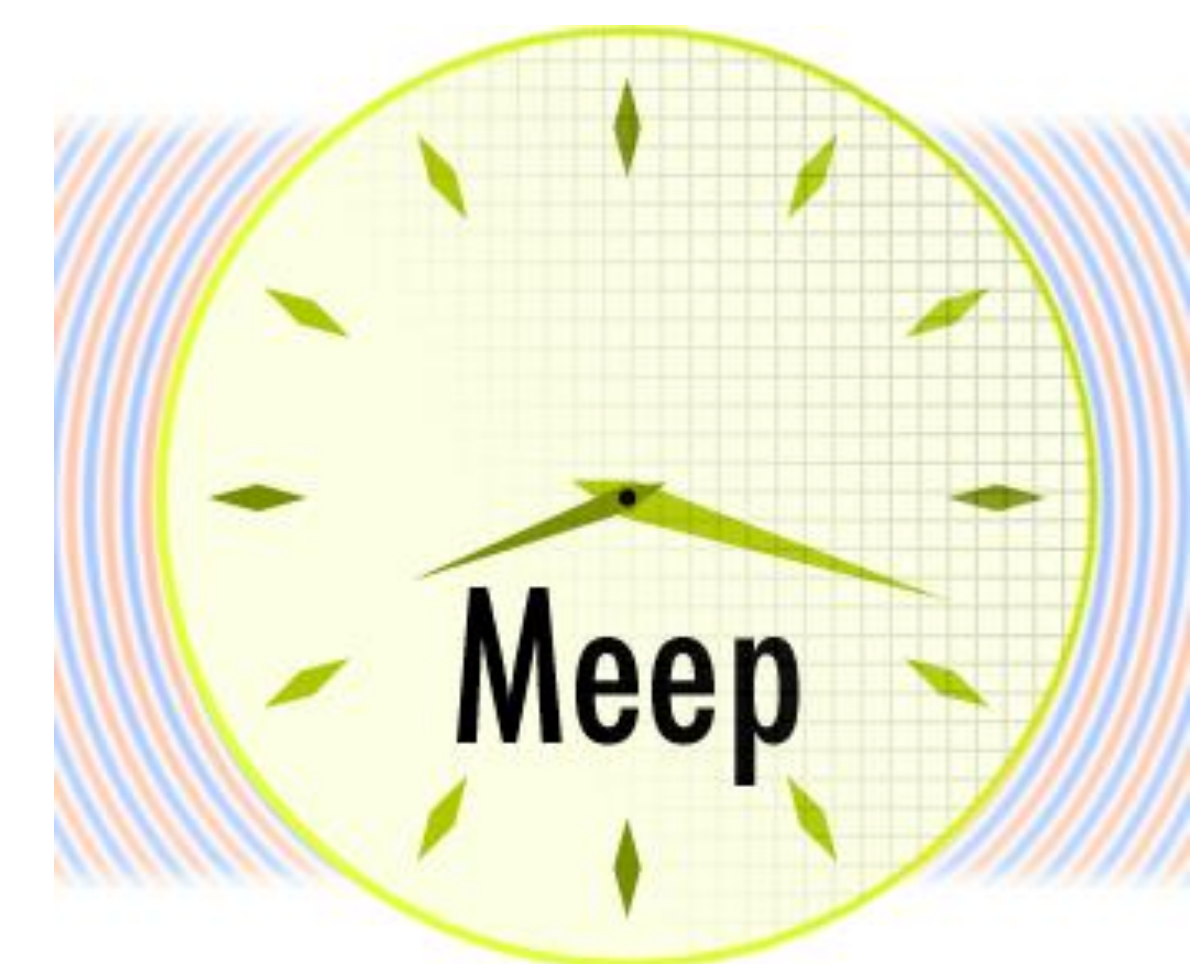
n_o : ordinary refractive index
 n_e : extraordinary refractive index
 V : applied voltage
 ϵ_0 : permittivity in vacuum

Geometry of 2x2 structure



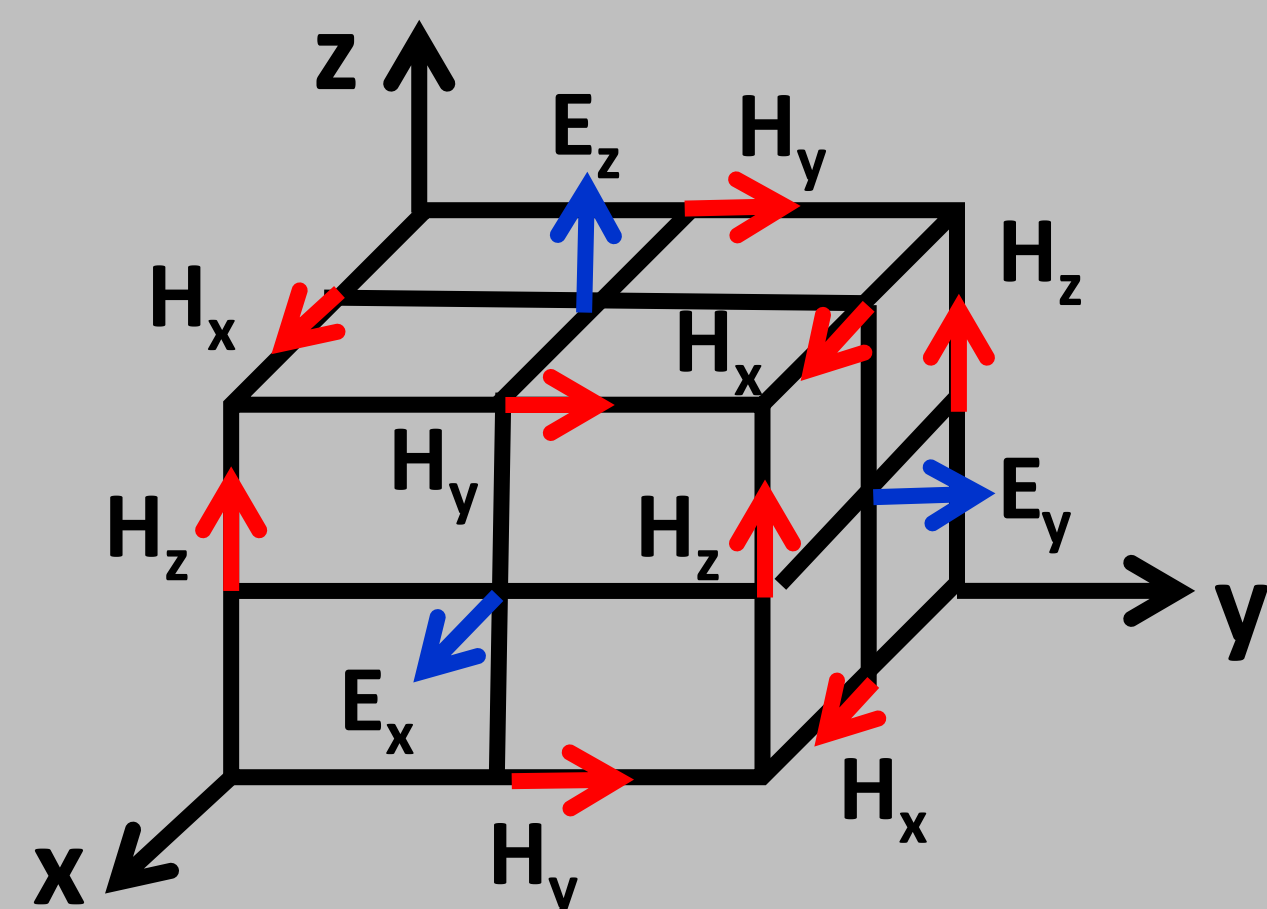
Simulation

1. Method: Finite-difference time-domain (FDTD) method
2. Open Source Software : MEEP, version 1.3



Main Theory behind FDTD method

1. Yee lattice



To maintain 2nd-order accuracy, E field are discretized and stored differently in space than H field, which also lead to divergence-free nature.

2. Unsplit perfectly matched layer

To handle the wave reflection from the anisotropic dispersive media at boundary, the following equations are used.

$$\begin{aligned} \bar{C}_k^{n+1} &= (1 + \sigma_D \Delta t / 2)^{-1} [(1 - \sigma_D \Delta t / 2) \bar{C}_k^n + \nabla \times \bar{H}_k^{n+0.5}] \\ \bar{U}_k^{n+1} &= (1 + \sigma_{k+1} \Delta t / 2)^{-1} [(1 - \sigma_{k+1} \Delta t / 2) \bar{U}_k^n + \bar{C}_k^n - \bar{C}_k^{n-1}] \\ \bar{D}_k^{n+1} &= (1 + \sigma_{k-1} \Delta t / 2)^{-1} [(1 - \sigma_{k-1} \Delta t / 2) \bar{D}_k^n + \bar{U}_k^n - \bar{U}_k^{n-1}] \\ \bar{W}_k^{n+1} &= \epsilon_\infty^{-1} (\bar{D}_k^{n+1} - \bar{P}_k^{n+1}) \\ \bar{E}_k^{n+1} &= \bar{E}_k^n + (1 + \sigma_k \Delta t / 2) \bar{W}_k^{n+1} - (1 - \sigma_k \Delta t / 2) \bar{W}_k^n \\ \bar{P}_k^{n+2} &= \chi_E(\omega) \bar{W}_k^{n+1} \end{aligned}$$

Δt = time step
 σ_D = conductivity
 ϵ_∞ = non-dispersive permittivity
 $\chi_E(\omega)$ = dispersive permittivity

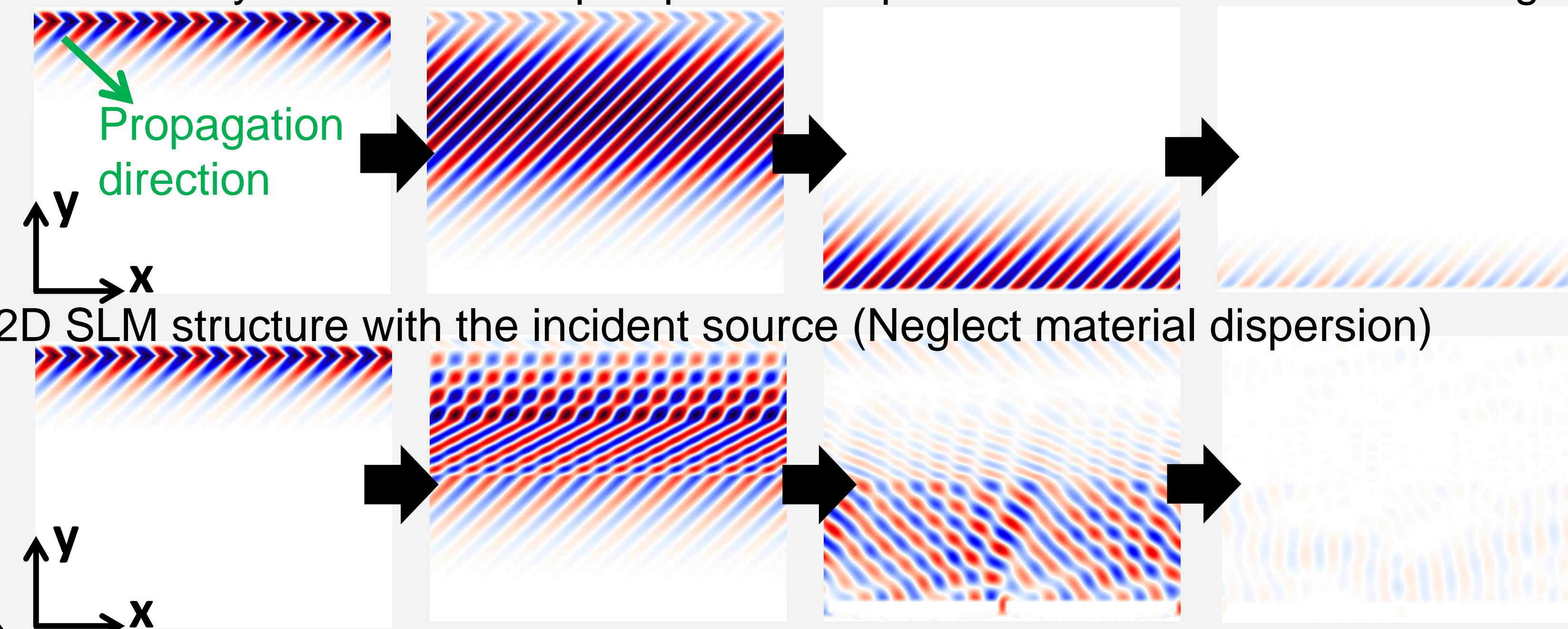
$k = x, y, z$ (direction, $k+1$ means shift of direction)

$n = 1, 2, 3, \dots$ (time steps)

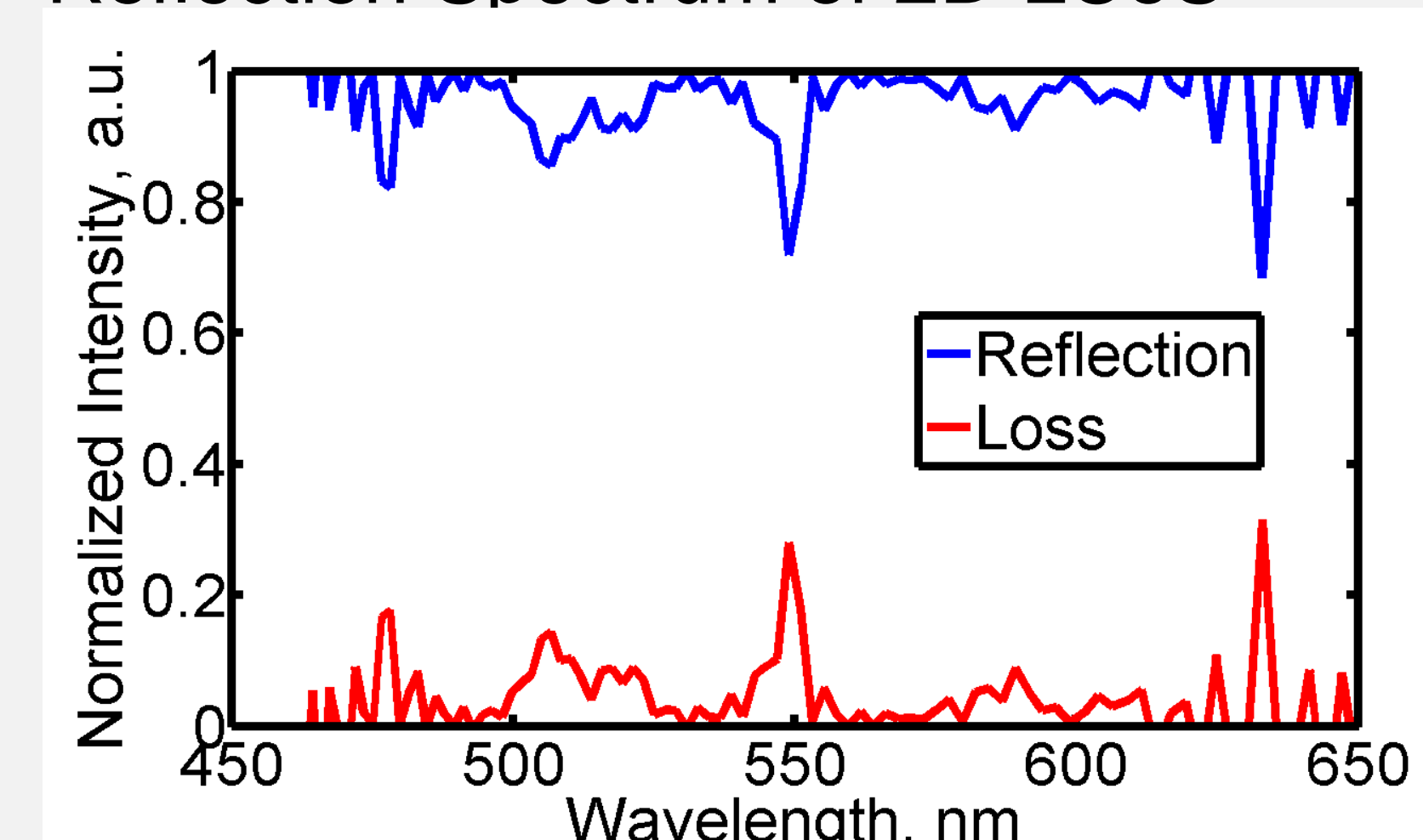
Preliminary results

We have always started from 2D structure for simplicity.

Source only : Gaussian-shaped pulsed TE plane wave with 45° incident angle



Reflection Spectrum of 2D LCoS



Key issues to deal with

1. Real 3D geometry
2. High requirement for the resolution (~nm) to get robust result

References

1. A. Taflove and S.C. Hagness, Computational Electrodynamics: The Finite-Difference Time-Domain Method (Artech House, third ed., 2005)
2. A. Oskooi and S.G. Johnson, Distinguishing correct from incorrect PML proposals and a corrected unsplit PML for anisotropic, dispersive media. J. Comput. Phys. 230 (7), 2369–2377 (2011)
3. MEEP, <https://meep.readthedocs.io/en/latest/>

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